

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ



السلام عليكم ورحمة الله وبركاته

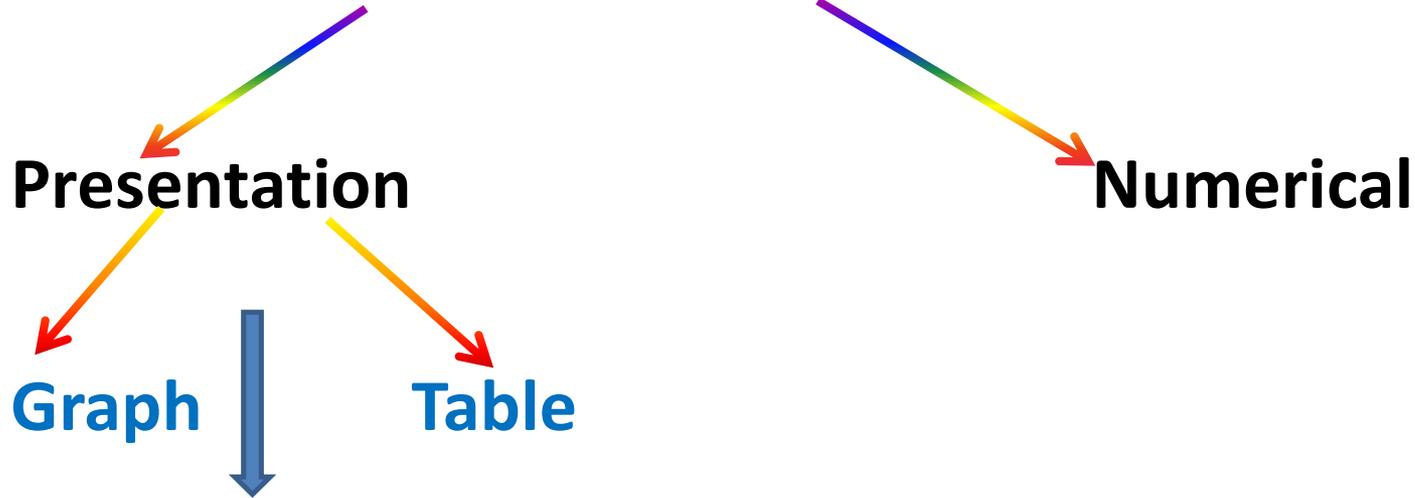
Biostatistics

LIV

12 –July 2023

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Description statistics summarization



- *this approach might not be enough,*
- *comparisons* between one set of data & another
- *summarize data by one more step further .*
- *presenting a set of data by a*
- *single Numerical value*

**The central value as
representative value in a set of data,**

1-Measures of central tendencies (Location) .

A value around which the data has a tendency to congregate (come together)or cluster

2-Measures of Dispersion, scatter around average

A value which measures the degree to which the data are or are not, spread out

The central value as

1-Measures of central tendencies (Location) .

A value around which the data has a tendency to congregate (come together)or cluster

2-Measures of Dispersion, scatter around average

A value which measures the degree to which the data are or are not , spread out

1-Measures of central tendencies (Location)

75, 75, 75, 75, 75, 75, Mean = ????

75, 70, 75. 80, 85. Mean = ????

60, 65, 55, 70, 75, 75, ,70, 80, Mean= ????

$$\bar{X} = \frac{\sum X}{N}$$

2-Measures of Dispersion,

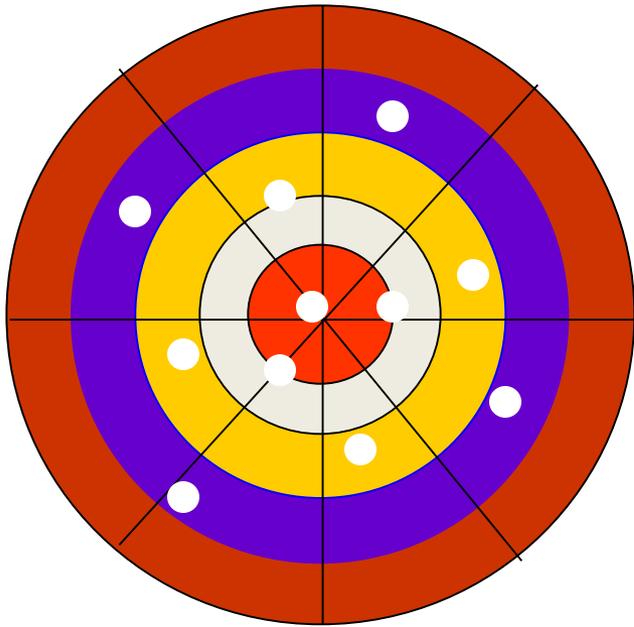
The central value as

1-Measures of central tendencies

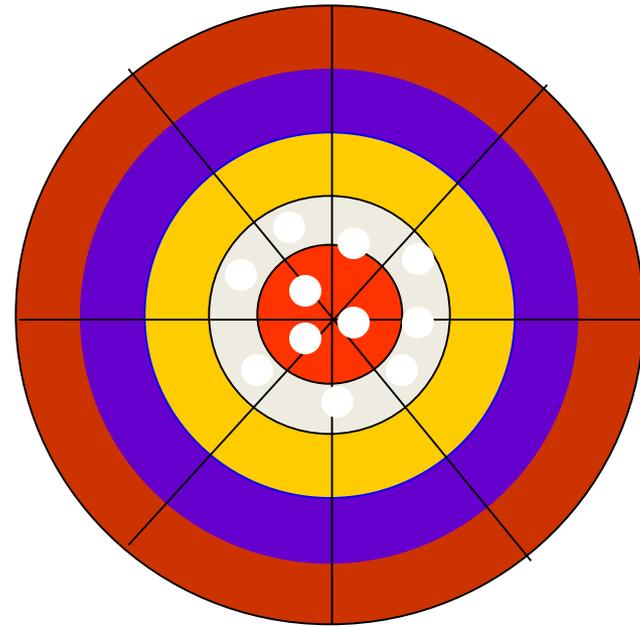
2-Measures of Dispersion,

Measures of Dispersion
(Measures of Variation)
(Measures of Scattering)
Measures of spread

Measures of Dispersion



SHOOTER A



SHOOTER B

*Both shooters are hitting around the “centre”
but shooter **B** is more “accurate”*

Measures of Dispersion

Measures of Dispersion
(Measures of Variation)
(Measures of Scattering)
measures of spread

1- Range

2- Interquartile range

3- Variance

4- Standard Deviation

5- Coefficient of variance

the choice of the most appropriate measure depends crucially on the **type of data** involved

Measures of spread

Measuring of spread are very useful.

There are three main measures in common use .

once again the type of data influence the choice of an appropriate measure

the choice of the most appropriate measure depends crucially on the **type of data** involved

- 1- Range
- 2- Interquartile range
- 3- Variance
- 4- Standard Deviation
- 5- Coefficient of variance

The Range

simplest

most obvious one of dispersion.

It is the distance from the **smallest** to the **largest**

It Obtained by

subtracting lowest value from the highest value in a set of data .

Pulse rate 70 76 74 78 72 74 76

Range = $78 - 70 =$

The range is **best written**

like range of data (from- to) 70-78

rather than single-valued difference which is much less informative

▪ The range is **not affected** by skewness

70 72 74 76 76 78 78 **78-70** 70-78

sensitive to the addition or removal of an **outlier** value

66 70 74 90, 100 120 124 124-66 **66-124**

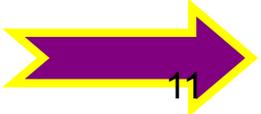
66 70 74 90, 100 120 124 **545** 66-545

Its disadvantage

it is based on **only two observations**
(the lowest and highest value) and

- ❖ give no idea about others,
- ❖ not take into consideration other values in data
- ❖ sensitive to an **outlier value** **Therefore**
- ❖ **It is not very useful** measures of variation,
- ✓ because it does **not use other** observation

Therefore ;



Therefore ;

Sensitive an outlier value

Interquartile rang (I q r).

- ✓ *measure the variation of one observation from the other*
- ✓ Standard deviation

Interquartile rang (I q r).



Percentile

A percentile provides information about **how the data** are spread over the interval from the smallest value to the largest value.

The **p th percentile** (25%) (30%):

is a value such that at least p percent of the observations are **less than or equal to this value** and at least **$(100 - p)$** (75%) (70%) percent of the observations **are greater than or equal to this value**.

The p th percentile is a value so that **roughly $p\%$ of the data are smaller** and **$(100-p)\%$ of the data are larger**.

Three Steps for computing a percentile.

- 1. Sort the data from low to high;**
- 2. Count the number of values (n);**
- 3. Select the $p^*(n+1)$ observation**

Examples

The following data represents cotinine levels in saliva (ng/ml) after smoking. We want to compute the 50th percentile.

73, 58, 67, 93, 33, 18, 147

Sorted data: 18, 33, 58, 67, 73, 93, 147

There are $n=7$ observations.

Select $0.50*(7+1)=4$ th observation.

Therefore, the **50th percentile equals 67.**

Notice that there are

three observations larger than 67 and

three observations smaller than 67.

Examples

The following data represents cotinine levels in saliva (ng/ml) after smoking. We want to compute the 20th percentile.

73, 58, 67, 93, 33, 18, 147

Sorted data: 18, 33, 58, 67, 73, 93, 147

Suppose we want to compute the **20th percentile**.

Notice that $p^*(n+1) = 0.20*(7+1)=1.6$. This is not a whole number so we select halfway **between 1st and 2nd** observation

they have to go **six tenths of the way to the** second value.

Calculation of percentile value

The p th percentile is
the value in the $p/100 (n+1)$ th position.

For example
the **20th percentile**

Calculation of percentile value

the birth weight (gram) of 30 infants which we put in ascending order.

| | | | | | | |
|------|------|------|------|------|------|------|
| 2860 | 2994 | 3193 | 3266 | 3287 | 3303 | 3388 |
| 3399 | 3400 | 3421 | 3447 | 3508 | 3541 | 3594 |
| 3613 | 3615 | 3650 | 3666 | 3710 | 3798 | |
| 3800 | 3886 | 3896 | 4006 | 4010 | 4090 | 4094 |
| 4200 | 4206 | 4490 | | | | |



Calculation of percentile value

The pth percentile is
the value in the $p/100 (n+1)$ th position.

the 20th percentile is the

$20/100(n+1)$ with the BW values

$20/100 (30 +1)$

0.2×31 observations = 6.2 observation

the birth weight of 30 infants which we put in ascending order.

| | | | | | | | | |
|------|------|------|------|------|------|------|------|------|
| 2860 | 2994 | 3193 | 3266 | 3287 | 3303 | 3388 | 3399 | 3400 |
| 3421 | 3447 | 3508 | 3541 | 3594 | 3613 | 3615 | 3650 | 3666 |
| 3710 | 3798 | 3800 | 3886 | 3896 | 4006 | 4010 | 4090 | 4094 |
| 4200 | 4206 | 4490 | | | | | | |



Cont. ..Calculation of percentile value

The 6th value is 3303 g
the 7th value is 3388 g

a difference of **85 g**

the 20th percentile is

3303 + 0.2 of 85 g

which is

$$3303\text{g} + 0.2 \times 85\text{ g} =$$

$$= 3303\text{g} + 17\text{g}$$

$$= \mathbf{3320\text{ g}}$$

the birth weight of 30 infants which we put in ascending order.

2860 2994 3193 3266 3287

3303 3388 3399 3400 3421 3447

3508 3541 3594 3613 3615 3650

3666 3710 3798 3800 3886

3896 4006 4010 4090 4094

4200 4206 4490

The pth percentile is

the value in the $p/100 (n+1)$ th position.

Similarly we could calculate

cont.Calculation of percentile value
the deciles

which subdivide the data values
into 10 (not 100)equal division,
and

Quintiles

which sub-divide the values into
five equal –sized groups

Collectively we call

❖ percentiles,

❖ **deciles** divide the sorted data into ten equal parts, so that each part represents 1/10 of the sample or population. **and**

❖ **quintiles**

the birth weight of 30 infants which we put in ascending order.

| | | | | | |
|------|------|------|------|------|------|
| 2860 | 2994 | 3193 | 3266 | 3287 | 3303 |
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The p th percentile is
the value in the $p/100 (n+1)$ th position.

A **quartile** is :

a division of observations into four defined 25% 50%

Interquartile rang (i q r).

One **solution** to the problem of the sensitivity to **extreme** value (**outlier**) is to

✓ **chop the quarter(25 percent)** of the values of **both ends** of the distribution

(which **removes** any troublesome **outliers**)

then measure the range of the remaining values

□ this distance is called

□ **interquartile range or i q r .**



Calculation of iqr

To calculate iqr we need to determine two values

first quartile (Q1)

The value which

**cuts off the bottom
25 percent of values**

third quartile (Q3)

The value which

**cuts off the top 25 percent of
values,**

The interquartile range is then written as (Q1 to Q3)

$$31 \times 0.25 = 7.75$$

$$31 \times .75 = 23.25$$

the birth weight of 30 infants which we put in ascending order.

| | | | | | | | |
|------|------|------|------|------|------|------|------|
| 2860 | 2994 | 3193 | 3266 | 3287 | 3303 | 3388 | 3399 |
| 3400 | 3421 | 3447 | 3508 | 3541 | 3594 | 3613 | 3615 |
| 3650 | 3666 | 3710 | 3798 | 3800 | 3886 | 3896 | 4006 |
| 4010 | 4090 | 4094 | 4200 | 4206 | 4490 | | |

The pth percentile is
the value in the $p/100 (n+1)$ th position.

with the BW data
 $Q1 = 3396.25\text{g}$ and
 $Q3 = 3923.50\text{g}$

$$\begin{aligned} 7.75^{\text{th}} \quad 3399 - 3388 &= 11 \times 0.75 = 8.25 + 3388 = \\ &3396.25 \\ 0.75 \times 31 &= 23.25^{\text{th}} \\ 4006 - 3896 &= 110 \times 0.25 = 27.5 + 3896 = 3923.5 \end{aligned}$$

the birth weight of 30 infants which we put in ascending order.

| | | | | | | | | |
|------|------|------|------|------|------|------|------|------|
| 2860 | 2994 | 3193 | 3266 | 3287 | 3303 | 3388 | 3399 | 3400 |
| 3421 | 3447 | 3508 | 3541 | 3594 | 3613 | 3615 | 3650 | 3666 |
| 3710 | 3798 | 3800 | 3886 | 3896 | 4006 | 4010 | 4090 | 4094 |
| 4200 | 4206 | 4490 | | | | | | |

Therefore iqr = 3369.25 to 3923.50)g

the middle 50 percent



Calculation of iqr

the middle **50 percent** of infant weighed
between **3396.25 and 3923.50 g**

✓ **The interquartile range**

indicate

- ❖ **the spread of the middle 50% of the distribution,**
- ❖ **together with the median is useful adjunct**
(accessory) to the range
- ❖ **it is less sensitive to the size of the sample**
providing that this is not too small

The interquartile range is not affected either by  Outlier
skewness

BUT

it does not use all of the information in the data set since it ignores the bottom and top quarter of values.

✓ *measure the variation of one observation from the other*

✓ Standard deviation





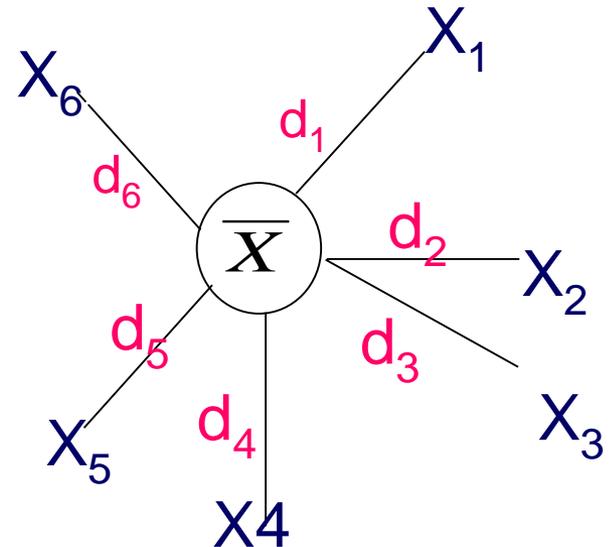
75, 70, 75. 80, 85.

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$$\bar{X} = \frac{\sum X}{N}$$

the **mean** (average) distance of all data values from the **over all mean** of all values.



Standard deviation (SD)

The limitation of iqr it does not use all of the information in the data since it omits the top and bottom quarter of values.

An alternative approach use the idea of summarizing spread by measuring the **mean** (average) distance of all data values from the **over all mean** of all values.

- **The smaller the mean distance is**
 - ✓ **the narrower the spread of values must be**
 - and visa versa**

this is known as **standard deviation**