

بِسْمِ اللَّهِ الرَّحْمَنِ الرَّحِيمِ



السلام عليكم ورحمة الله وبركاته

# Biostatistics

L III

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# **Numerical Presentation**

## **Numerical Description**

**Measures of Central Tendency**

**Measures of Dispersion**

This include:

## Presentation of data by

~~1. Graph and or~~

~~2. Tables~~

3. **Calculation** or numerical summaries, such as  
Frequency, Average, Mean, Median, Mode  
Percentages

Biostatistics consist of

- 1-Collection of data .
- 2-Presentation of data
- 3-.Estimation of data

Descriptive statistics



# Description statistics summarization

Presentation

Numerical

Graph

Table

- *this approach might not be enough,*
- *comparisons* between one set of data & another
- *summarize data by one more step further .*
- *presenting a set of data by a*
- *single Numerical value*

# **Numerical Presentation**

## **Numerical Description**

**1-Measures of Central Tendency**

**2-Measures of Dispersion**

## Example

The following data representing age (years) of 50 patients with diabetes Mellitus collected from Al Karak Hospital during march 2023

68, 62, 62, 66, 68, 65, 64, 71, 77, 74, 20, 33, 38. 42, 47.  
50, 55, 56, 60 72, 80 74, 75, 74, 77, 80, 81, 89, 86, 85,  
83, 72, 70, 71, 79, 76, 77, 80, 90, 97, 94, 90, 65, .60, 67,  
63 88, 84, 84, 87

7

**An important thing is the type of the variable concerned.**

# The central value as representative value in a set of data

## 1-Measures of central tendencies (Location) .

A **value** around which the data has a tendency to congregate (come together )or cluster

## 2-Measures of Dispersion, scatter around average

A **value** which measures the degree to which the data are or are not, **spread** out

-single Numerical value. ??

Are we using **largest** value ?

Are we using **lowest** value ?

As a single Number  
representation

**The central value as  
representative value in a set of data,**

# The central value as representative value in a set of data

## 1-Measures of central tendencies (Location) .

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# Measures of Central Tendency

A value around which the data has a tendency to **congregate** or **cluster**

1- Mean

2- Median

3- Mode

4- weighted mean

the choice of the most appropriate measure **depends** crucially on the **type** of data involved

# Mode (Mo)

❖ **Most frequently** occurring value in a set of observation

5 1, 3, 2, 6, 7, 10 **5** ??????

Or

❖ the value of observation which has the **highest frequency** in a set of observation .

**1** 5 1, 3, 1, 2, 6, 7, 10 5 ??????

❖ **Mode is the only measure** of central tendency that can be used for **qualitative data** ???

❖ is **not practically** useful with the **metric continuous** data where no two value may be the same,

➤ If the observation all having different value

5 1, 3, 2, 6, 7, 10 ??????

So



the observation all having different value

there is **no Mode** 5 1 3 2 6 .

We might have **one Mode** 5, (1) 2, 3, 1, 6 uni modal

We might have more than one Mode

(5), 1, (3), 5 7, 3, 6, 2 **Two Mode** Bimodal

(5), (1), (3), 5, 7, 3, 6, 2, 1 **Three Mode** Tri modal

5, 1, 3, 5, 7, 3, 6, 2, 1, 3 ???

3

uni modal

# Characteristics of Mode

## Advantages and Disadvantages

1-Requires no calculation just counting

2- It may not exist (No Mode)

3-It is not necessarily be unique

there may be one mode **unimodal**

more than one mode in a set of data

**Bimodal, Tri modal ....**

- It is the **only measure** of central tendency that can be used for **qualitative data**

4 -Mode is **not practically** useful with the **metric continuous data**

## Median ( Md )

It is the **middle value** in **ordered data**  
(*from the lowest to the highest values* ).

-**Divided the observations into two halves** .

*So*

- ❖ **1/2** of observation their values **less** than the **value of median**
- ❖ **1/2** of observation their values **More** than the **value of median**
- ❖ Median is located the center of data **by count** and **disregards the size** .
- ❖ Median is thus a measure of centrals

## Steps in calculating the median

### 1- Arrange the value.

From the lowest to the highest value .

Exam. marks

50 10 90 20 40  10 20 40 50 90

### 2- Find the Median position by this formula

$$\frac{n + 1}{2} = \frac{5 + 1}{2} = 3^{rd}$$

Calculate the value of the third observation = 40 marks .

**Odd No.** we have just **one median position** .

**Even No.** we have **two median position** or  
**two median values**

**Median value = Average of the two values**



Even No    50   10   90   20   40   95

10    20    40    50    90    95

$$\frac{n + 1}{2} = \frac{6 + 1}{2} = \frac{7}{2} = 3.5$$

Median **located (position)**

**between the 3<sup>rd</sup> and 4<sup>th</sup>.**

Median value = **Average** of the two (3<sup>rd</sup> and 4<sup>th</sup>) values

$$Md = \frac{40 + 50}{2} = 45$$

# Characteristics

10	20								
20	40	50	90	95					
10	20	40	50	90	95	99	100	.....	

10	20	40	50	70	85	90	99	100
1	20	40	50	70	85	90	99	100
10	20	40	50	70	85	90	99	1000.

two extremes

15	20	30	35	95	99	100
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skewness

1	5	10	35	400	900	1000
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# Characteristics of the Median

It is always existed .

- ❖ It is always **unique**, there is one and only one  $Md$  .
- ❖ It is not affected by two extremes, not sensitive by two extremities .
- ❖ Not affected by skewness in the distribution or
- ❖ Not affected by presence of outliers
- ❖ It is discard a lot of information because it ignores most of the values apart from those in the center of distribution

# Mean

 $\bar{X}$ 

## Arithmetic Mean

- ❖ more commonly known as average
- ❖ -it is an arithmetic average of a set of observation

### obtained by

- Adding the values of all observation together .
- Dividing the sum by No. of observation in sample .
- *It represent the center of data according to the size of the values .*

### Example :

following are the scores of five students

40

50

90

10

20

 $\bar{X}$  $\equiv$ 

$$\frac{\sum X}{N}$$

$$\overline{X} = \frac{\sum X}{N}$$

$\Sigma$  = sigma = summation .

$X$  = value of observation

$N$  = No. of observation

$\overline{X}$

= is the sum of value of all observation  
divided by the total No. of observation

# Characteristics of the Mean

## Advantages and disadvantages

- Relatively easy to handle
- It is **always exist**
- It is **always unique**,  
there is one and only one Mean
- It takes into account every item in a set of data
- It uses all of the information in the data set.
- **affected by skewness** in the in the data set
- **affected by presence of outliers**
- it can not be used with the ordinal data ???



➤ **It is affected by the two extremes by a very small or a very large value .**

➤ **It is sensitive to the extremes**

**1    2    3    4    5    mean = 3**

**1    2    3    4    50    mean = 12**

**1    2    3    4    500    mean = 102**

➤ **this may produce a mean that is not very representative of the general mass of data**

**another disadvantage ,**

➤ **it can not be used with the ordinal data ???**

**(ordinal data are not real numbers,  
so they cannot be added or divided )**

## Weighted mean

It is the average measure of a No. of means, when we take into consideration the frequencies of each mean .  
It is used when some values of observation more important in some sense than others .

$$W.mean = \frac{W_1 \bar{X}_1 + W_2 \bar{X}_2 + W_3 \bar{X}_3 + \dots + W_k \bar{X}_k}{W_1 + W_2 + W_3 + \dots + W_k}$$

Group	$\overline{X}$ Hb	No. of person
I	13	5
II	14	10
III	13.5	15

$$W.mean = \frac{5 \times 13 + 10 \times 14 + 15 \times 13.5}{5 + 10 + 15} = \frac{407.5}{30} = 13.5 \text{ gm/100 ml}$$

$$\frac{65 + 140 + 202.5}{5 + 10 + 15} = \frac{407.5}{30} = 13.58$$

## Central Tendency In Grouped Data

Age (year)	F	M.P.	(M.P.)F	Cum. F	%
20-29	2	24.5	24.5 2 = 49	2	4
30-39	8	34.5	34.5 8 = 276	10	16
40-49	5	44.5	44.5 5 = 222.5	15	10
50-59	14	54.5	54.5 14 = 763	29	28
60-69	15	64.5	64.5 15 = 967.5	44	30
70-79	6	74.5	74.5 6 = 447	50	12
total	50	---		---	100

$$\sum (\text{M.P.})F = 2725$$

$$2725/50 = 54.5$$

years

# Choosing the most appropriate measure

(Mean, Median or mode)

How do you choose the most appropriate measure of location in a given set of data ??

The main thing is to remember is that



*mean can not be use with the ordinal data* ( because they are not real numbers

the median can be use for both ordinal & metric data.

**the Median can be use for both ordinal & metric data.**

when the later (**metric data**)  
is skewed

Or

when there is outlier

**the median is**  
more representative of data than the mean

????????

	Mode	Median	Mean
Nominal	<b>Yes</b>	<b>No</b>	<b>No</b>
Ordinal	<b>Yes</b>	<b>Yes</b>	<b>No</b>
Metric discrete	<b>Yes</b>	<b>Yes if distribution is markedly skewed</b>	<b>yes</b>
Metric continuous	<b>No</b>	<b>Yes if distribution is markedly skewed</b>	<b>yes</b>



1-Measures of central tendencies (Location) .

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# The central value as

## 1-Measures of central tendencies (Location)

75, 75, 75, 75, 75, 75, Mean = ????

75, 70, 75, 80, 85. Mean = ????

60, 65, 55, 70, 75, 75, ,70, 80, Mean= ????

$$\overline{X} = \frac{\sum X}{N}$$

## 2-Measures of Dispersion,

The central value as

1-Measures of central tendencies

2-Measures of Dispersion,

# Measures of Dispersion (Measures of Variation) (Measures of Scattering) measures of spread