



Biostatistics

* Mid :

$$1- \text{Relative frequency} = \frac{\text{No. of frequencies of each cent...}}{\text{total frequency}}$$

$$2- \text{Percentage frequency} = R.f \times 100\%$$



غير مطابق في حساب الكلام المذكورة

$$3- \text{Sturges rule (K)} = 1 + 3.322 (\log N)$$

No. of classes \rightarrow تتسق لاجل

$$4- \text{Width of class interval} = \frac{\text{Range}}{k}$$

$$5- \text{Mid point} = \frac{X_1 + X_2}{2}$$

* Measurements of Central tendency :

1- Mode (M_o)

$$2- \text{Median (Md)} \Rightarrow \frac{n+1}{2}$$

$$3- \text{Mean } (\bar{X}) = \frac{\sum_{i=1}^n X_i}{N}$$

$$4- \text{Weghred mean} = \frac{W_1 X_1 + W_2 X_2 \dots + W_k X_k}{W_1 + W_2 \dots + W_k}$$

disadvantage = limitation = negativity

* Measures of dispersion

1- Range (أقصى - أقل قيمة) \cong (أبسط قيمة - أقل قيمة)

$$2- \text{Variance } (S^2) = \frac{\sum (X - \bar{X})^2}{N-1}$$

$$3- \text{Standard deviation} = \pm \sqrt{S^2} \quad \text{or} \quad S.D = \sqrt{\sum X^2 - \frac{(\sum X)^2}{N}} / (N-1)$$

$$4- C.V = \frac{S.D}{\bar{x}} * 100 \%$$

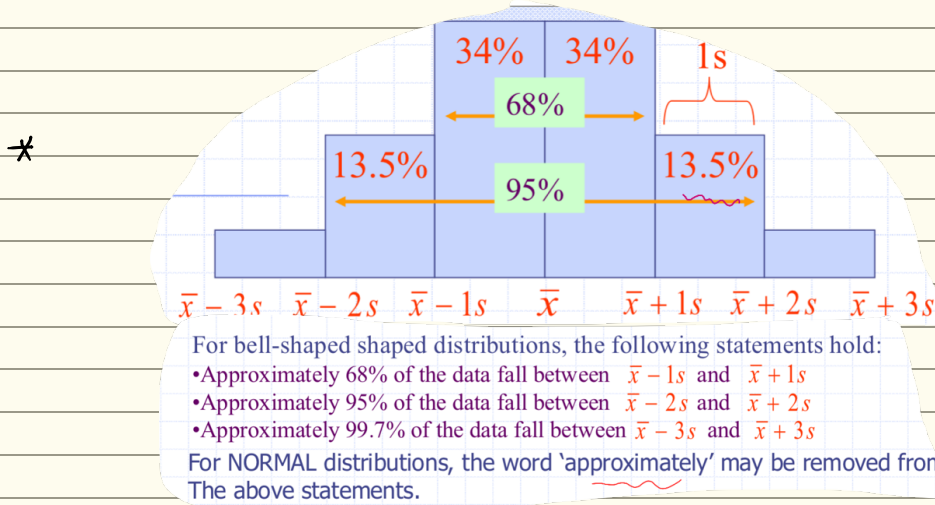
$$* \text{ Standard error} = \frac{S.D}{\sqrt{N}}$$

* حيث N هي حجم العينة
في اد group الواحد.

$$* \text{ 91 within 95\%} = \bar{x} \pm 1.96 S.E$$

$$\Rightarrow 95\% \text{ of Conf. interval} = \bar{x} \pm 1.96 S.E$$

$$* \text{ 91 within 99\%} = \bar{x} \pm 2.58 S.E$$



* * الأفضل خلال الامتحان
رسم الرسمة ...

$$* Z = \frac{X_i - \bar{X}}{S.D}$$

* x-scale \rightarrow abscissa

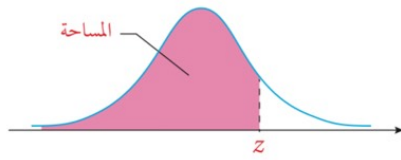
* y-scale \rightarrow ordinate

\rightarrow to transform the X value to its corresponding Z value.

* If we want to represent the distribution of averages as a standard normal we use the :

$$Z = \frac{\bar{X}_i - \bar{X}}{S.D/\sqrt{n}} = \frac{\bar{X}_i - \bar{X}}{S.E}$$

* للاختصار *



$$* P(Z > a) = 1 - P(Z < a)$$

جدول التوزيع الطبيعي المعياري

z	0.00	0.01	0.02	0.03	0.04	0.05	0.06	0.07	0.08	0.09
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517
0.4	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224
0.6	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7517	0.7549
0.7	0.7580	0.7611	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852
0.8	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133
0.9	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015
1.3	0.9032	0.9049	0.9066	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177
1.4	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633
1.8	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	0.9706
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890
2.3	0.9893	0.9896	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952
2.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964
2.7	0.9965	0.9966	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981
2.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986
3.0	0.9987	0.9987	0.9987	0.9988	0.9988	0.9989	0.9989	0.9989	0.9990	0.9990
3.1	0.9990	0.9991	0.9991	0.9991	0.9992	0.9992	0.9992	0.9992	0.9993	0.9993
3.2	0.9993	0.9993	0.9994	0.9994	0.9994	0.9994	0.9994	0.9995	0.9995	0.9995
3.3	0.9995	0.9995	0.9995	0.9996	0.9996	0.9996	0.9996	0.9996	0.9996	0.9997
3.4	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9997	0.9998

$$* P(Z < -a)$$

$$= P(Z > a) = 1 - P(Z < a)$$

$$* P(a < Z < b)$$

$$= P(Z < b) - P(Z < a)$$

* Final :

1- Degree of freedom (df) = $n-1$

2- Calculated $t = \frac{\bar{x} - \mu}{S.E}$ (SE = $\frac{SD}{\sqrt{N}}$)

To test a sample of normal continuous data, we need:

1. An expected value = the population or true mean
2. An observed mean = the average of your sample
3. A measure of spread: standard error
4. Degrees of freedom (df) = $n-1$ (number of values used to calculate SD or SE)

Then, we can calculate a test statistic to be compared to a known distribution

Keep these concepts in your mind.

3- \hookrightarrow if $p\text{-value} \geq \alpha \rightarrow$ accept the Null. ((fail to reject))

\hookrightarrow if $p\text{-value} < \alpha \rightarrow$ reject the Null.

4. \hookrightarrow if calculated $t >$ critical $t \rightarrow$ reject the Null.

\hookrightarrow if calculated $t <$ critical $t \rightarrow$ accept the Null.

* p-value : مقياس - اختباري يقي احتمال أن تكون النتائج التي حصلنا عليها في تجربة أو دراسة ما عن العينة نوعاً.

OR p-value represent the area that corresponds to the z or the t-test statistic.

* $\alpha \rightarrow$ probability of type I error (reject the H_0 | H_0 is true)

* يعني بتخيري هل النتائج أجنبية بالصدفة ولا لا؟

\hookrightarrow مثلاً لو $P=0.05$ هنا يعني أن احتمال أن نتناهي

ما في 100 احتمال تكون نتائجنا نتيجة من غيرنا بعض الصدفة.



← طبعاً في حالة
تصبح ونحن في النوع أو خاطئ

مثال خطأ

5- The test considered statistically significant when we reject the Null

$\hookrightarrow (p\text{-value} < \alpha)$

6- = = = insignificant

when we accept the Null Hyp.

$\hookrightarrow (p\text{-value} > \alpha)$

2 samples

* For independent t-test: (unpaired)

$$* df = (n_1 + n_2) - 2$$

$$* \text{pooled variance} = \frac{S_1^2 (n_1 - 1) + S_2^2 (n_2 - 1)}{(n_1 + n_2) - 2}$$

$$* \text{calculated } t = \frac{\bar{X}_1 - \bar{X}_2}{\sqrt{\frac{S^2_p}{n_1} + \frac{S^2_p}{n_2}}}$$

* For dependent t-test (paired):

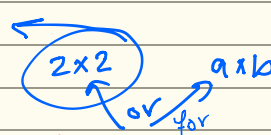
one sample // (Before + After)
(مقارنة قبل وبعد)

$$* t = \frac{\bar{X}_D - \mu_0}{S.E. \left(\frac{S_D}{\sqrt{n}} \right)}$$

μ₀ = population mean difference

$$* df = n - 1$$

الأفضل كلاً



* Chi-Square :

- 1- independent.
- 2- qualitative variable.
- 3- Dichotomous (yes/no) (نعم/لا) variable.

↳ the assumption of it: 1- mutually exclusive (متباين) (50% yes or 50% no)
2- the count of each cell must not be less than 5. (if less use Fisher best.)

$$* df = (r-1)(c-1)$$

$$* \chi^2 = \sum \frac{(O-E)^2}{E}$$

$$* E = \frac{\text{total } c \times \text{total } r}{\text{Ground total}}$$

* Continuity Correction (Yates) :

$$\chi^2 = \sum \frac{(|O - E| - 0.5)^2}{E}$$

* Used when $df = 1$
 ↳ means just for
 2x2 table.

↳ resulting in small value
 for chi square.

↳ يعني بيكون متأكد أكثر من
 النتيجة.

* القانون للنتيجة

* (P_0) → true proportion (Rate) for total

* P_1 → Rate (proportion) succeeded

	♂	♀	total
succeeded	70 87.5%	90 75%	160 80%
not succeeded	10 12.5%	30 25%	40
Total	80	120	200

If the true population proportion of condition is

$$160/200 = 0.8 \quad 40/200 = 0.2$$

$P_0 = 0.8$ and

Rate (proportion) of succeeded ♂ (p_1) = $70/80 = 87.5\%$

Rate (proportion) of succeeded ♀ (p_2) = $90/120 = 75\%$

$$H_0 = P_1 = P_2 = P_0$$

$$H_A = P_1 \neq P_2 \neq P_0$$

????



3. SUMMARY OF STATISTICAL TESTS:

CATEGORICAL DATA	Enough data	Too little data (<5 in a cell)
Any r x c table	Chi-square	Fisher's Exact
CONTINUOUS DATA	Normal (even if transformed to normal) or large n	Not normal: (non-parametric tests)
One (group) sample	1-sample t-test	Kolmogorov-Smirnov
Two samples	2-sample t-test	Mann-Whitney U or Rank Sum
Paired data	1-sample t-test on paired differences (paired t-test)	Wilcoxon Signed-Rank
Three or more samples	Analysis of variance (ANOVA)	Kruskal-Wallis

* Incidence rate = $\frac{\text{No. of persons developing a disease in a specific time and locality} \times 1000}{\text{Total No. of population at risk}}$

(new cases)

* Prevalance rate = $\frac{\text{No. of persons who has the disease (existing) in a specific time and locality}}{\text{Total No. of population at risk}} \times 1000$

Analysis of Case Control

	مصاب Cases	غير مصاب Control	total
مرضى Exposed	A	B	A+B
غير مرضى Non	C	D	C+D

Odds Ratio = $\frac{A}{B} \div \frac{C}{D} = \frac{AD}{BC}$

السبب بين المرضين السبب بين غير المرضين

* Odd Ratio = $\frac{\text{Exposed}}{\text{Non Exposed}} = \frac{\frac{A}{B}}{\frac{C}{D}} = \frac{AD}{BC}$

في الخلية استمارة

تفسير النسبة الاحتمالية:

- إذا كانت النسبة الاحتمالية = 1: هذا يعني أنه لا يوجد فرق في الاحتمالات بين المجموعتين.
- إذا كانت النسبة الاحتمالية < 1: هذا يعني أن التعرض للعامل يزيد من احتمال حدوث النتيجة.
- إذا كانت النسبة الاحتمالية > 1: هذا يعني أن التعرض للعامل يقلل من احتمال حدوث النتيجة.

Analysis of cohort :

* Estimation of risk :

Relative Risk (RR) = $\frac{\text{Incidence of disease among exposed}}{\text{Incidence of disease among non-exposed}} = \frac{\frac{a}{a+b}}{\frac{c}{c+d}}$