

$$1) r = 1.12 \times 10^{15} \sqrt[3]{238} = 7.43 \times 10^{15}$$

### HW 6

$$2) v_{\alpha} = 0.05c \\ v_{\beta} = 0.9c$$

$$\frac{v_{\beta}}{v_{\alpha}} = \frac{0.9}{0.05} = 18$$

$$v_{\beta} = 18 v_{\alpha}$$

- Find the radius of a  $^{238}\text{P}$  nucleus.
- What is the ratio of the velocity of a  $\beta$  particle to that of an  $\alpha$  particle, if they have the same nonrelativistic kinetic energy?
- The decay constant of  $^{235}\text{U}$  is  $9.8 \times 10^{-10} \text{ y}^{-1}$ . (a) Calculate the half-life. (b) How many decays per second occur initially in a  $1.0\text{-g}$  sample of  $^{235}\text{U}$ ? (c) How many  $^{235}\text{U}$  nuclei will remain in the  $1.0\text{-g}$  sample after  $10^9 \text{ y}$ ?
 

$T_{1/2} = \frac{0.693}{\lambda} = 2.23 \times 10^6 \text{ y}$   
 $\lambda = 9.8 \times 10^{-10} \text{ y}^{-1}$   
 $N = N_0 e^{-\lambda t} = 2.52 \times 10^6 e^{-9.8 \times 10^{-10} \times 10^9} = 9.61 \times 10^4 \text{ nuclei}$
- $^{62}\text{Cu}$  is produced at a constant rate in a reactor and decays by  $\beta$  decay with a half-life of about 10 min. How long does it take to produce 90% of the maximum possible number of  $^{62}\text{Cu}$ ?
 

$\lambda = \frac{0.693}{10} = 0.0693 \text{ min}^{-1}$   
 $0.9 N_{\infty} = N_0 (1 - e^{-\lambda t})$   
 $0.9 = 1 - e^{-\lambda t} \Rightarrow e^{-\lambda t} = 0.1$   
 $-\lambda t = \ln(0.1) \Rightarrow t = \frac{-\ln(0.1)}{\lambda} = \frac{2.303}{0.0693} = 33.2 \text{ min}$
- The half-life of  $^{227}\text{Th}$  is 18.72 d. It decays by  $\alpha$  emission to  $^{223}\text{Ra}$ , an  $\alpha$  emitter whose half-life is 11.43 d. A particular sample contains  $10^6$  nuclei of  $^{227}\text{Th}$  and no  $^{223}\text{Ra}$  at  $t = 0$ . How many nuclei of  $^{223}\text{Ra}$  will be in the sample at  $t = 15 \text{ d}$ ?
- A sample of animal bone discovered at an archeological site is found to contain 175 g of carbon, and the decay rate of  $^{14}\text{C}$  in the sample is measured to be 8.1 Bq. How old is the bone?
- 350 rads of  $\alpha$ -particle radiation is equivalent to how many rads of X-rays in terms of biological damage?
 

$1 \text{ rad } \alpha \rightarrow 20 \text{ rad X-rays}$   
 $350 \text{ rad } \alpha \rightarrow 7000 \text{ rad X-rays}$
- A dose of 4.0 Sv of rays in a short period would be lethal to about half the people subjected to it. How many grays is this?
 

$\text{Effective dose (Sv)} = \text{Dose (Gy)} \times \text{RBE}$   
 $4 \text{ Sv} = \text{Dose (Gy)} \times 1$   
 $\text{Dose} = 4 \text{ Gray}$
- How many rads of slow neutrons will do as much biological damage as 72 rads of fast neutrons?
- How much energy is deposited in the body of a 65-kg adult exposed to a 4.5-Gy dose?

Type	RBE
X- and $\gamma$ rays	1
$\beta$ (electrons)	1
Protons	2
Slow neutrons	5
Fast neutrons	$\approx 10$
$\alpha$ particles and heavy ions	$\approx 20$

$$6) 175 \rightarrow N_0$$

$$N_0 = 75.25 \times 10^{23}$$

$$T_{1/2} = 5730 \text{ y}$$

$$\lambda = \frac{0.693}{5730 + 365 \times 21 \times 360} = 3.835 \times 10^{-12}$$

$$R = \lambda N$$

$$N = \frac{R}{\lambda} = \frac{8.1}{3.83 \times 10^{-12}} = 2.112 \times 10^{12}$$

$$N = N_0 e^{-\lambda t}$$

$$t = 7.536 \times 10^{12} \text{ s} = 238,960 \text{ yr}$$

$$9) \quad \begin{array}{l} 1 \text{ fast} \longrightarrow 10 \text{ } \mu\text{-rays} \\ 72 \text{ fast} \xrightarrow{\quad} \mu \end{array}$$

$$\mu = 720$$

1:1

$$\begin{array}{l} 1 \text{ Slow} \longrightarrow 5 \text{ } \mu\text{-rays} \\ \text{Num slow} \xrightarrow{\quad} 720 \end{array}$$

$$\mu = \frac{720}{5} = 144 \text{ rad s}$$


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$$10) \quad 1 \text{ gray} = 1 \text{ J / kg}$$

$$4.5 \text{ gray} = \text{Energy}$$

$$\text{Energy} = 4.5 \text{ J / kg}$$

$$\text{Energy} = 4.5 (65) = 292.5 \text{ J}$$